

**Jet Propulsion Laboratory**  
California Institute of Technology

# Multi-Frequency Radar Retrieval of Snowfall Microphysics

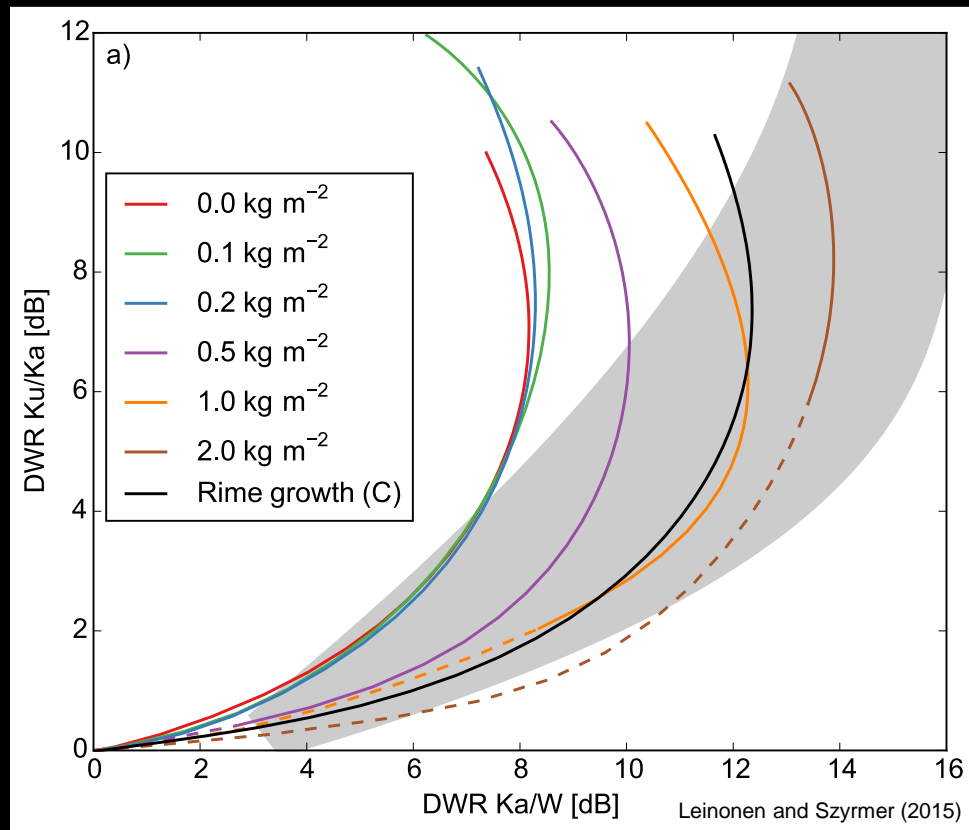
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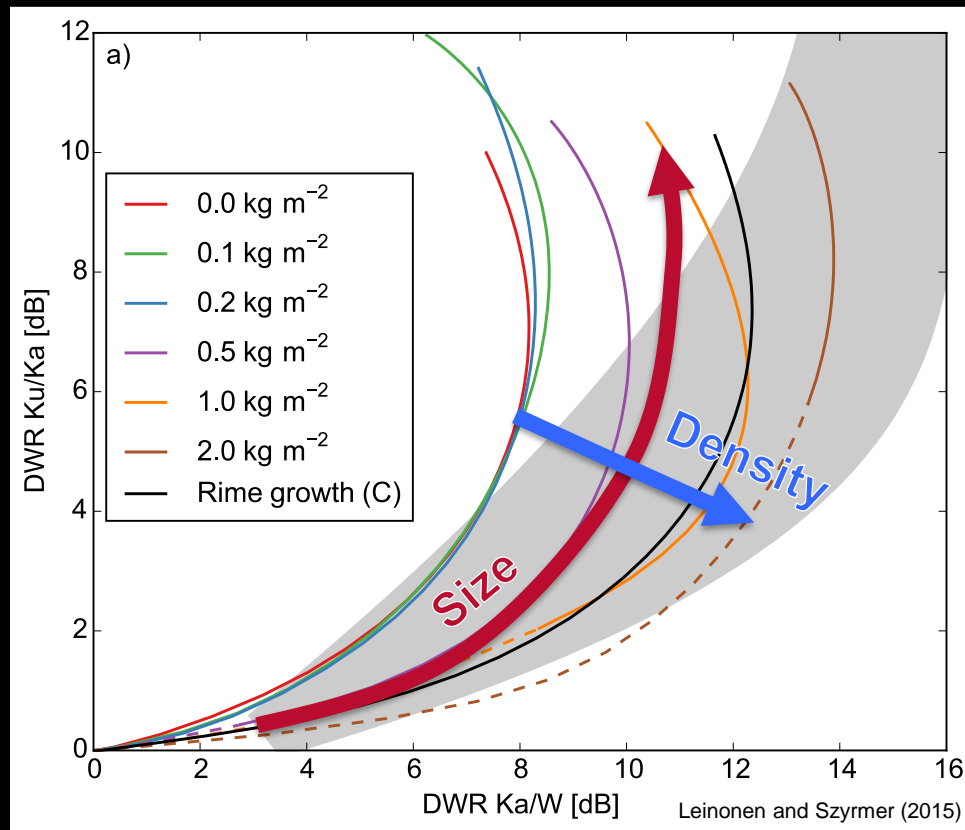
# Multi-frequency retrievals

- Single frequency: *water content*
- Dual-frequency: *hydrometeor size*
- Triple-frequency: *snow density*



# Multi-frequency retrievals

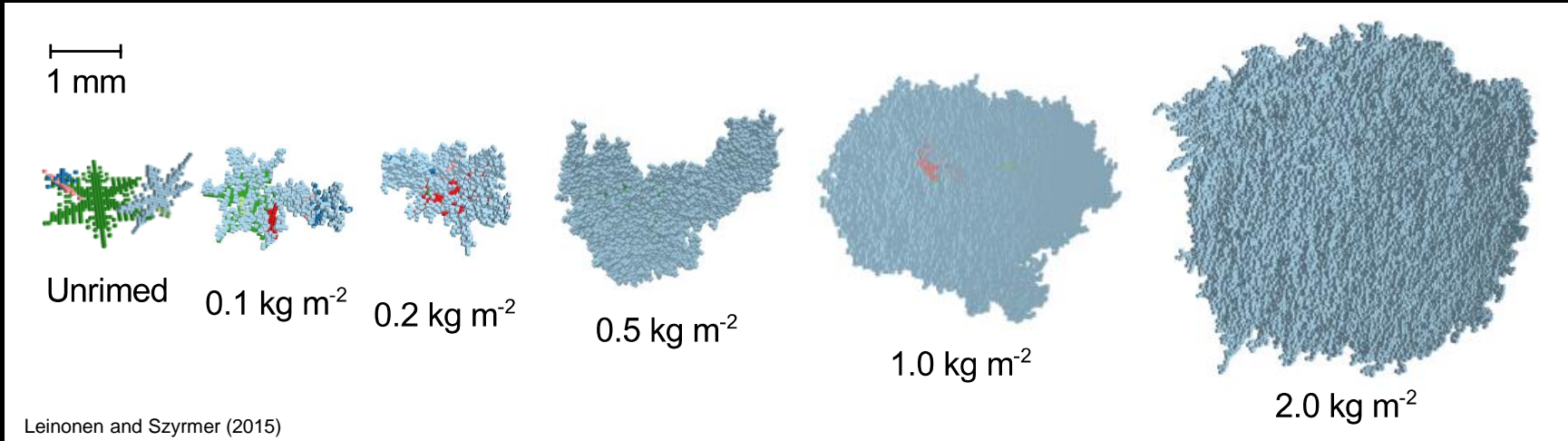
- Single frequency: *water content*
- Dual-frequency: *hydrometeor size*
- Triple-frequency: *snow density*



# Multi-frequency retrievals

Now available:

- Triple-frequency data from campaigns
- Snow scattering databases with variable density





# Algorithm

$$E[\mathbf{x}|\mathbf{y}] = \int \mathbf{x} p(\mathbf{x}|\mathbf{y}) d\mathbf{x} = \frac{1}{p(\mathbf{y})} \int \mathbf{x} p(\mathbf{y}|\mathbf{x}) p(\mathbf{x}) d\mathbf{x}$$

Measurement:

$$\mathbf{y} = \begin{bmatrix} Z_{\text{dB,Ku}} \\ \text{DWR}_{\text{Ka/W}} \\ \text{DWR}_{\text{Ku/Ka}} \end{bmatrix}$$

State:

$$\mathbf{x} = [\ln N_0 \quad \ln \Lambda \quad \ln \alpha]^T$$

$$N(D) = N_0 \exp(-\Lambda D)$$

$$m(D) = \alpha D^\beta$$

# Algorithm

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Forward model +  
Measurement error

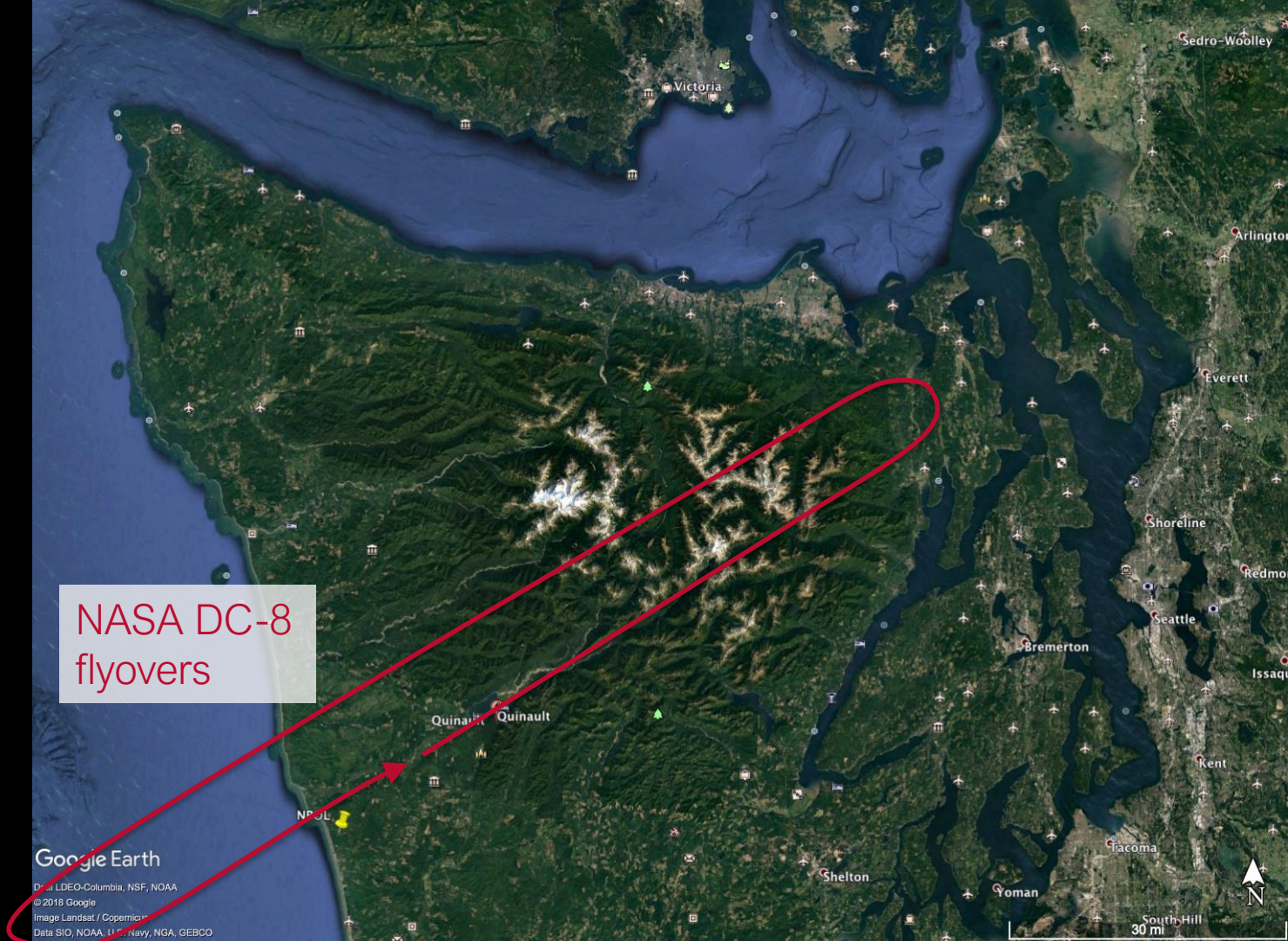
*A priori* probability  
(from field measurements)

# OLYMPEX

NASA DC-8  
flyovers

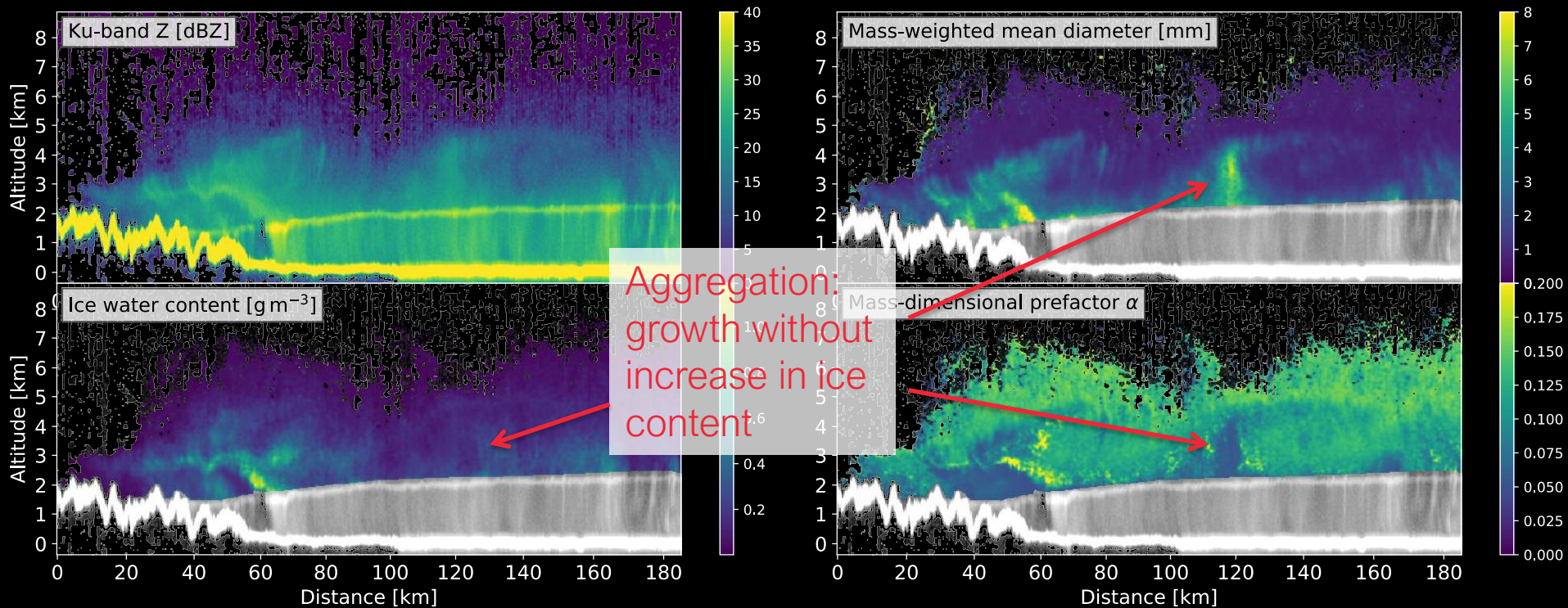
Google Earth

Data LDEO-Columbia, NSF, NOAA  
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Image Landsat / Copernicus  
Data SIO, NOAA, U.S. Navy, NGA, GEBCO



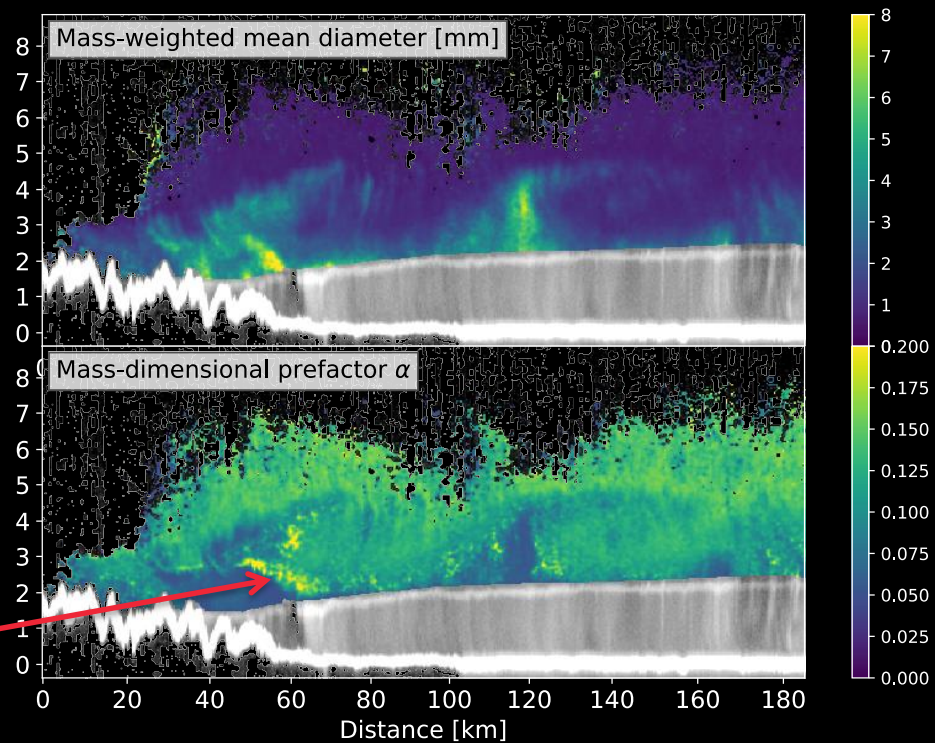
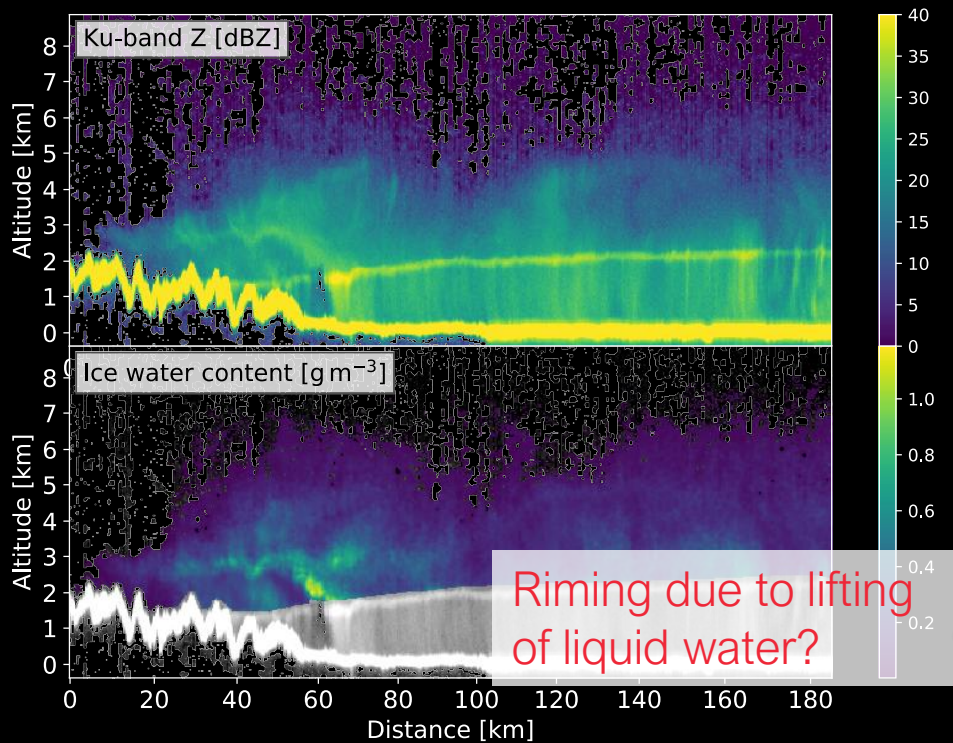


# December 1, 2015

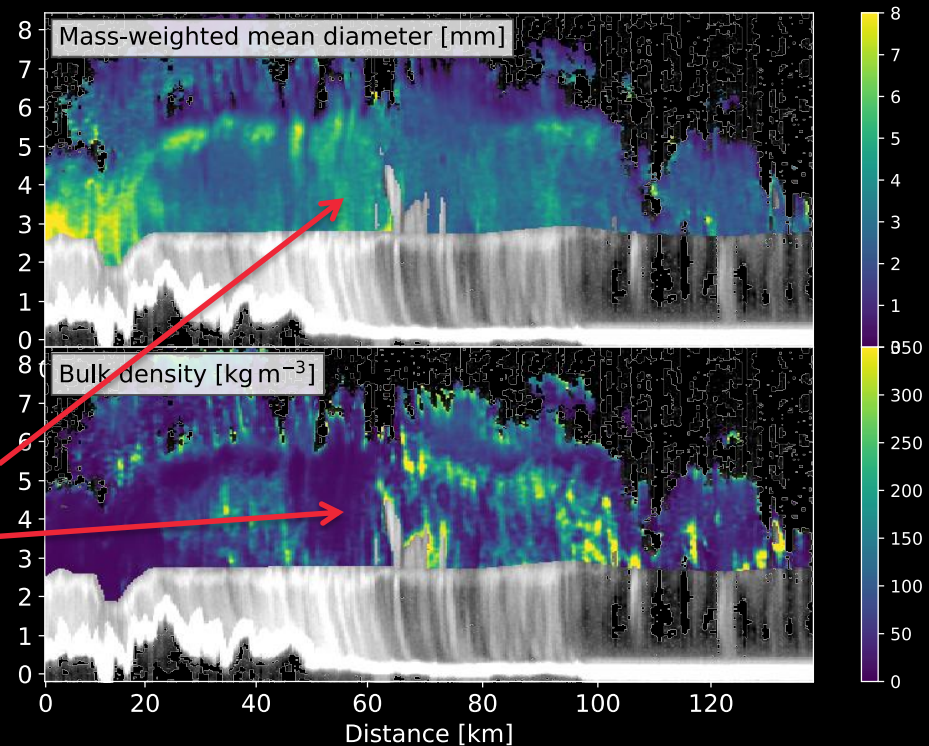
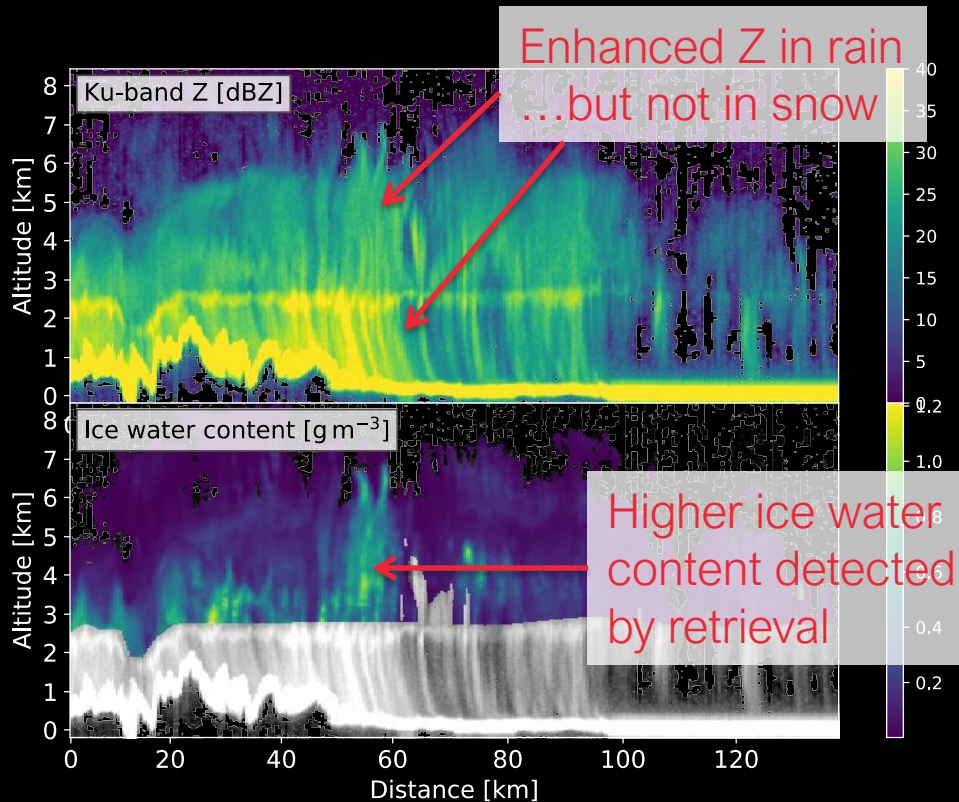




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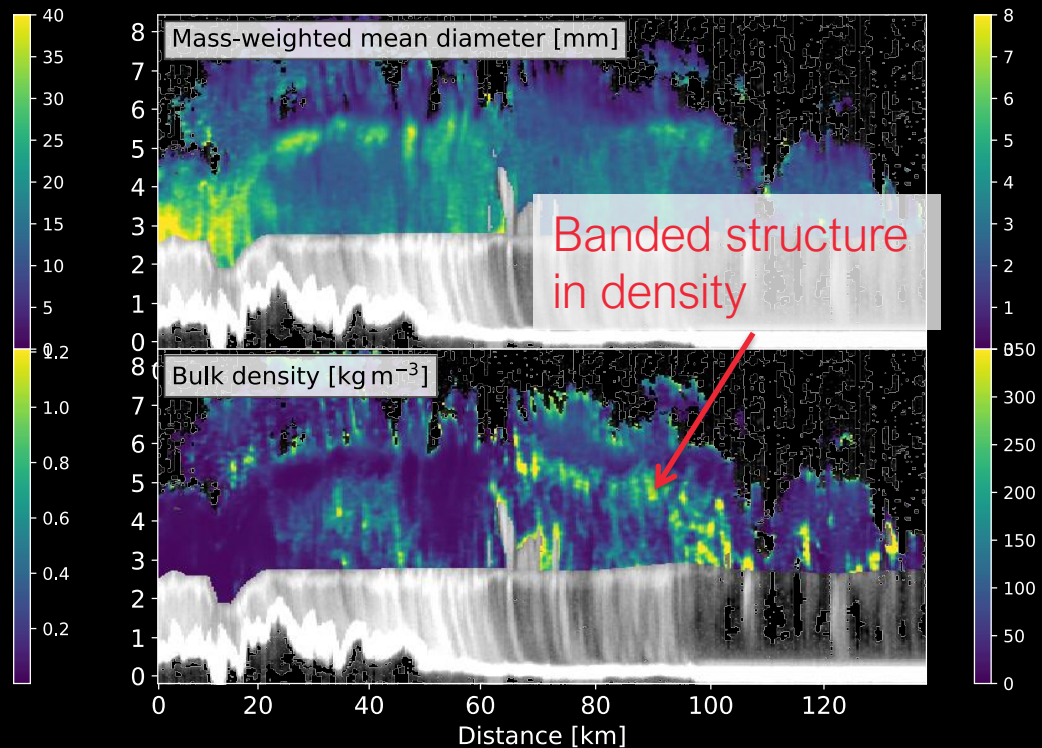
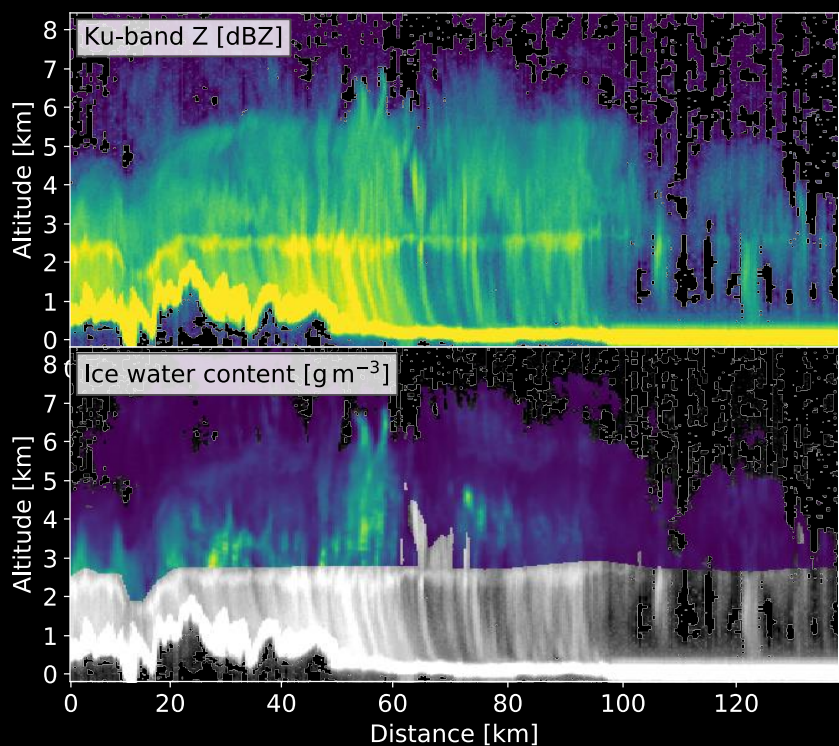


# December 8, 2015

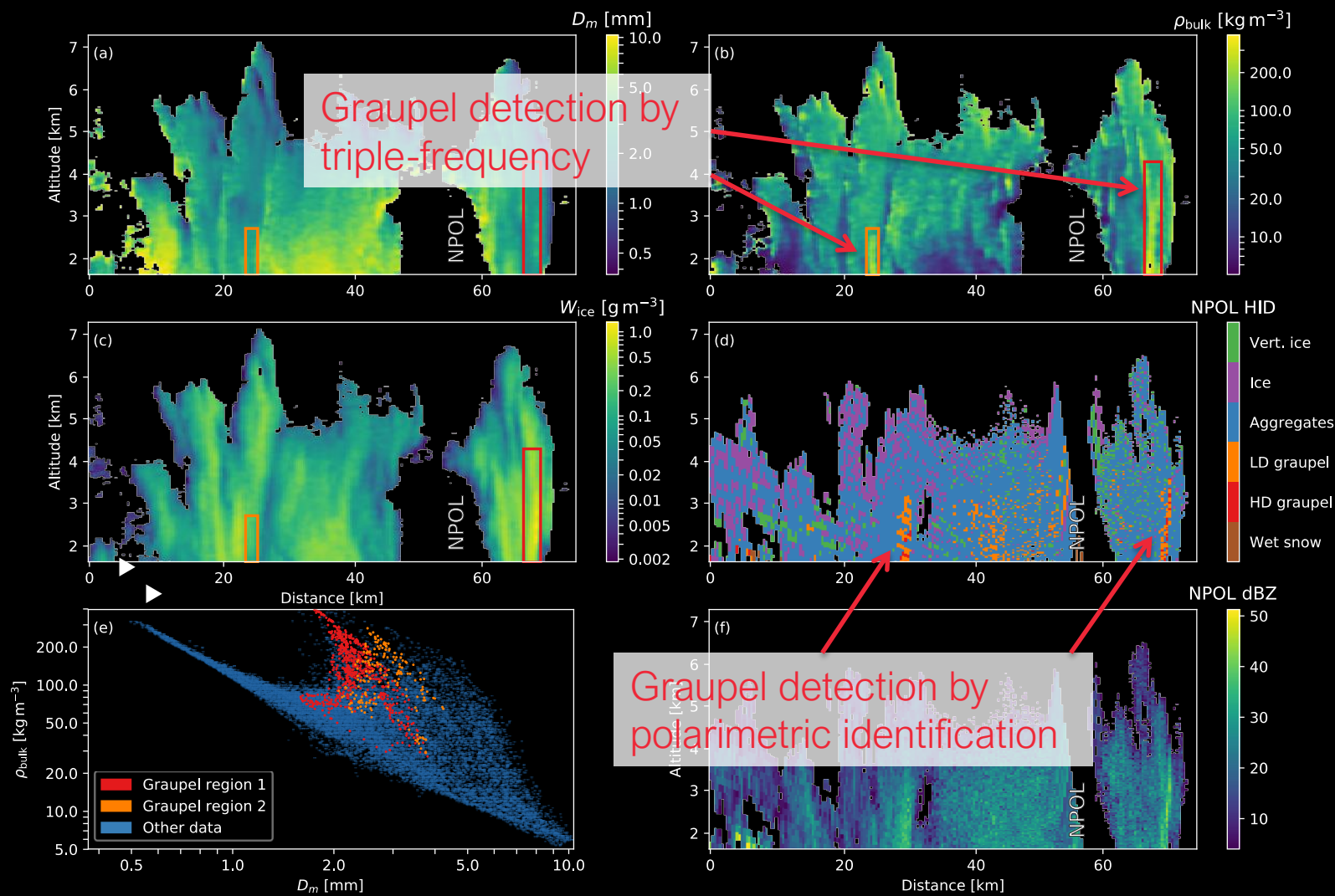




# December 8, 2015



Dec 4,  
2015



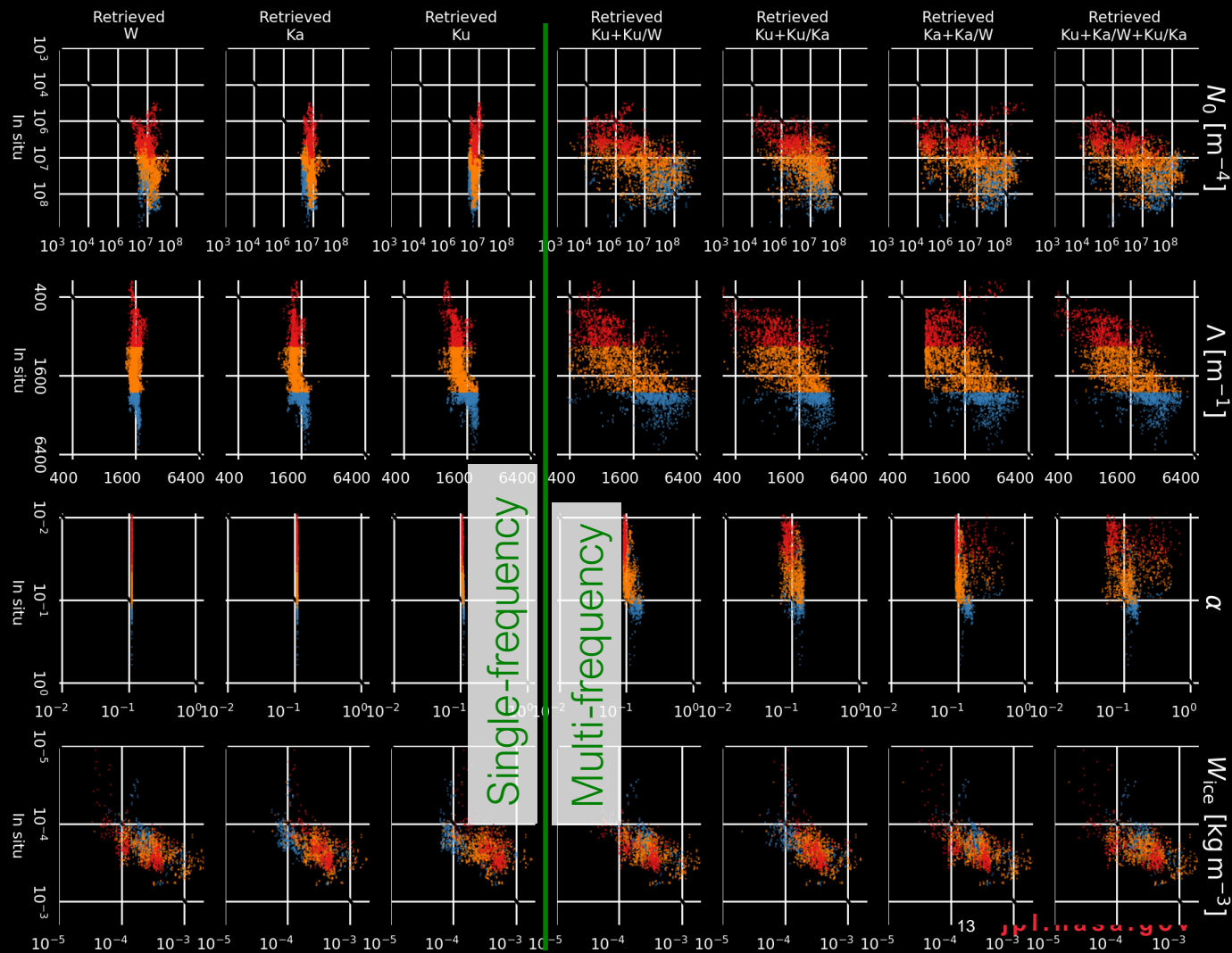


# Comparisons to in-situ data

Size ▶

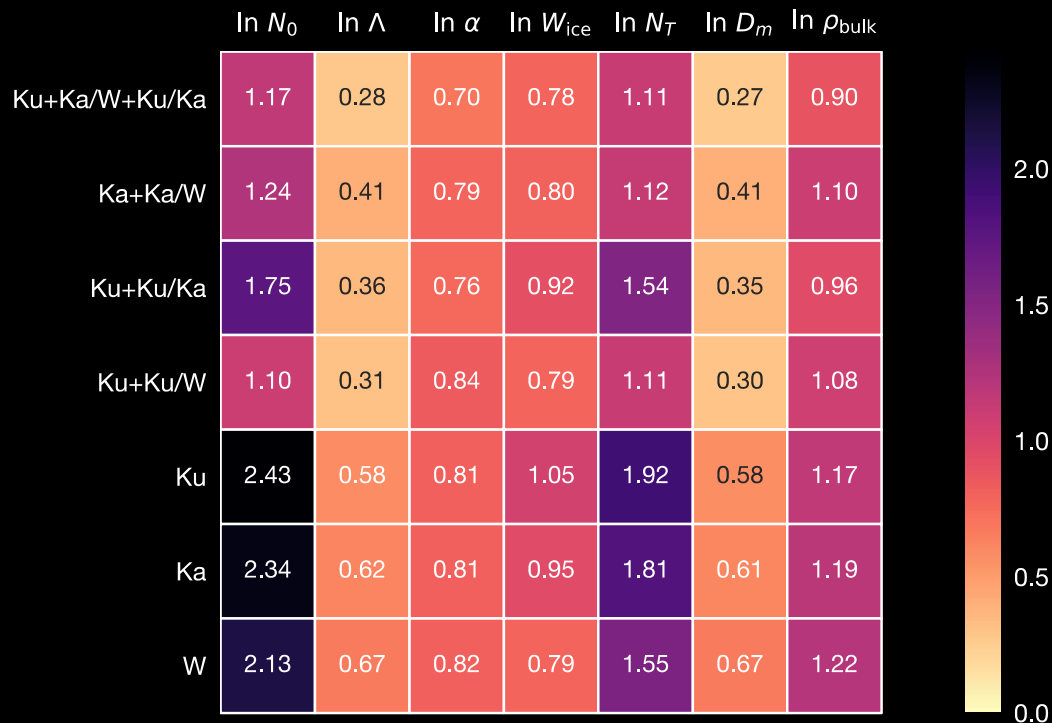
Density ▶

Ice water content ▶



# Error estimates

- Size and number concentration better constrained by multi-frequency
- Differences in ice water content and density errors are small



# Summary

- Multi-frequency retrieval algorithm for ice and snow microphysics
  - Uses snowflake scattering models of varying densities
  - Can identify processes such as aggregation and riming
  - Tested with OLYMPEX airborne 3-frequency radar data
  - Multi-frequency retrievals improve performance for size and number concentration vs. single frequency



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